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Numerical Solutions of Integral Equations Using Linear Legendre Multiwavelets

Meenu Devi¹ · Sunil Rawan² ⑤ · Vineet Kishore Srivastava³ · Sushil Chandra Rawan⁴

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Abstract

This paper presents a novel approach for solving Fredholm integral equations and Fredholm integro-differential equations using an operational matrix of integration based on linear Legendre multiwavelets. By employing this operational matrix, we transform the integral equations into a system of algebraic equations, significantly simplifying the solution process. To validate the effectiveness of our method, we solve several illustrative examples and provide graphical comparisons of approximate solutions against exact solutions. Additionally, we conduct a comparative analysis of our results with those obtained using the Wilson wavelet method and the Cosine and Sine wavelet method, which are presented in tabular form. The results demonstrate that the proposed method not only enhances accuracy but also improves computational efficiency in solving these complex equations.

 $\textbf{Keywords} \ \ Linear \ Legendre \ multiwavelets \cdot Operational \ matrix \ of \ integration \cdot Integral \ equations$

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Sunil Rawan sunilrawan2710@gmail.com Meenu Devi meenurathore.nakur@gmail.com Vineet Kishore Srivastava vk_srivastava78@yahoo.co.in Sushil Chandra Rawan sushilchandrarawan@gmail.com

- Department of Mathematics, Kirori Mal College, University of Delhi, Delhi 110007, India
- Department of Mathematics, Balganga Degree College, Sendul, Kemar, Ghansali, Tehri Garhwal, Uttarakhand 249155, India
- Department of Mathematics, School of Applied and Life Sciences, Uttaranchal University, Dehradun, Uttarakhand 248007, India
- Department of Mathematics, School of Applied and Life Sciences, Uttaranchal University, Dehradun, Uttarakhand 248007, India